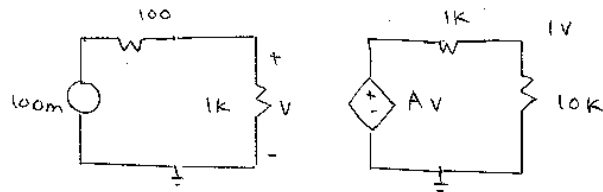


5. A voltage amplifier (with voltage gain  $A$ , input resistance of  $1\text{ k}\Omega$  and output resistance of  $1\text{ }\Omega$ ) is used to amplify a  $100\text{ mV}$  voltage source (with source resistance of  $100\text{ }\Omega$ ) to give a  $1\text{ V}$  output across a  $10\text{ k}\Omega$  load. Sketch the circuit model of the source-amplifier-load circuit and hence show that  $A = 12.1$ . (16)

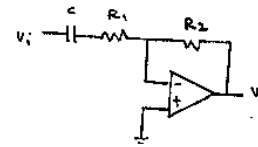


$$1 = AV \frac{10\text{K}}{1\text{K}}$$

$$= A \cdot 100\text{m} \cdot \frac{1\text{K}}{100} \cdot \frac{10\text{K}}{1\text{K}}$$

$$\therefore A = 12.1$$

7. In the ideal op amp circuit, show that  $H = V_o/V_i = -R_2 / (R_1 + 1/j\omega C)$ . If  $C = 1\text{ }\mu\text{F}$ ,  $R_1 = 2\text{ k}\Omega$  and  $R_2 = 10\text{ k}\Omega$ , find the magnitude of  $H$  ( $|H|$ ) when  $\omega = 0$ ,  $1/CR_1$  and  $\infty$ . Hence sketch  $|H|$  versus  $\omega$ . What filter is it? (27)



$$\frac{V_i - 0}{Z_1} = \frac{0 - V_o}{Z_2}$$

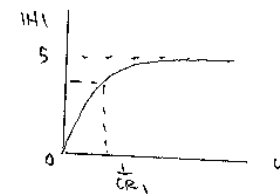
$$\therefore \frac{V_o}{V_i} = -\frac{Z_2}{Z_1} = -\frac{R_2}{R_1 + \frac{1}{j\omega C}} = H \quad 6$$

$$|H| = \frac{\frac{R_2}{R_1}}{\sqrt{1 + \left(\frac{1}{\omega C R_1}\right)^2}} \quad 3$$

$$\omega = 0 \quad |H| = 0 \quad 4$$

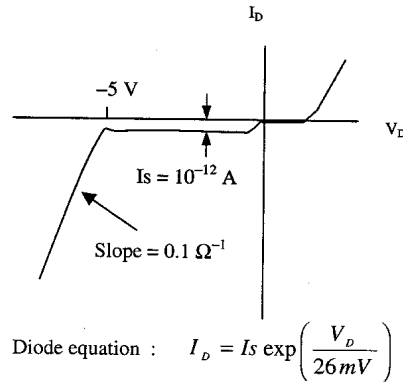
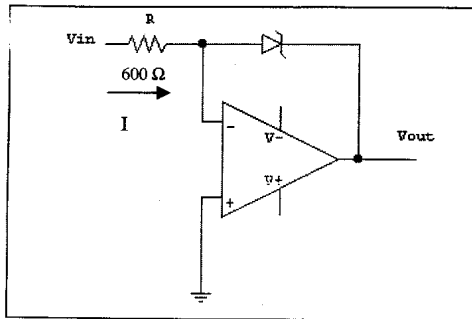
$$\omega = \infty \quad |H| = \frac{R_2}{R_1} = 5 \quad 4$$

$$\omega = \frac{1}{CR_1} \quad |H| = \frac{\frac{R_2}{R_1}}{\sqrt{2}} = \frac{5}{\sqrt{2}} \quad 4$$

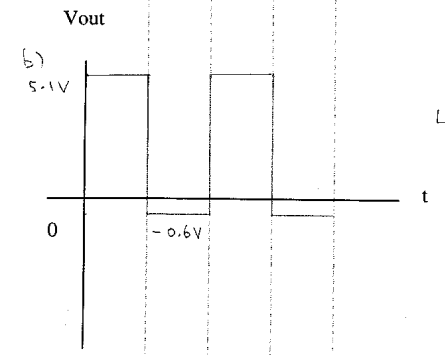
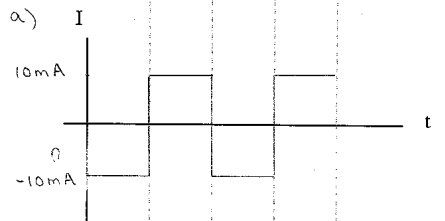
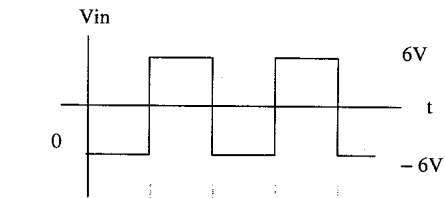


high pass filter

7. Given the following circuit diagram, the input voltage  $V_{in}$  and the I-V characteristics of the zener diode.



- a) Sketch the current  $I$ . Show your calculations clearly. (6 marks)  
b) Sketch the output voltage  $V_{out}$ . Show your calculations clearly. (20 marks)

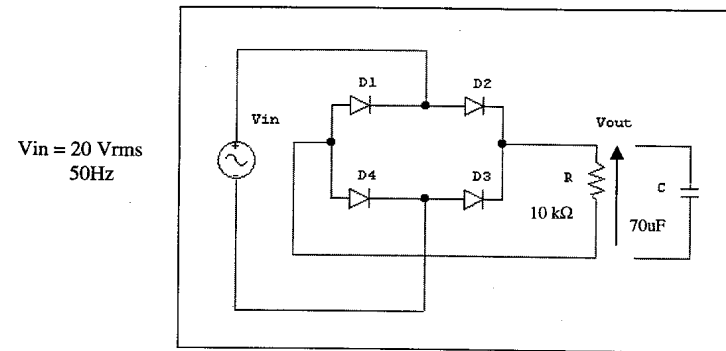


$$\begin{aligned} a) \quad I &= \frac{V_{in}}{R} \\ &= \frac{6V}{600} \\ &= 10mA \end{aligned} \quad 2$$

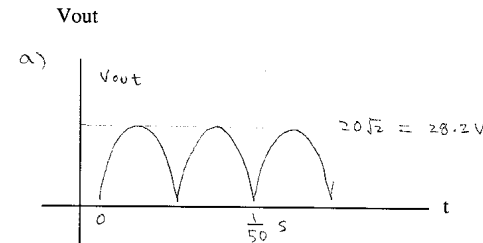
$$\begin{aligned} b) \quad I &= 10mA \\ \text{diode is forward biased} \\ I &= 10mA = I_S e^{\frac{-V_D}{26mV}} \\ \therefore V_D &= -0.6V \end{aligned} \quad 8$$

$$\begin{aligned} I &= -10mA \\ \text{diode is breakdown} \\ V_D &= 5 + \frac{10mA}{0.1} \\ &= 5.1V \end{aligned} \quad 8$$

8. Given the following ideal diode circuit diagram.



- a) Sketch the output voltage  $V_{out}$ . Show clearly the voltage and time intercepts. (5 marks)  
b) Calculate the DC voltage  $V_{DC}$  across  $R$  ( $V_{DC} = 2V_m / \pi$ ). (3 marks)  
c) Find the peak inverse voltage (PIV) of the diode. (4 marks)  
d) Show that the ripple voltage  $V_r = 0.4V$  after a capacitor of  $70\mu F$  is connected across  $R$ . (6 marks) Justify the assumption that you used. (3 marks)  
e) Estimate the DC voltage across  $R$  after the capacitor is added. (4 marks)



$$b) \quad V_{DC} = \frac{2V_m}{\pi} = \frac{2(28.2)}{\pi} = 18V \quad 3$$

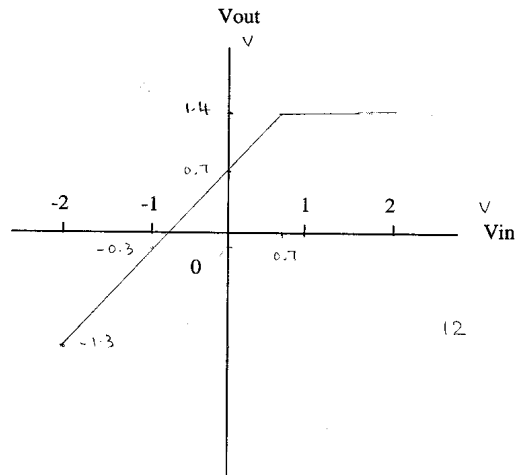
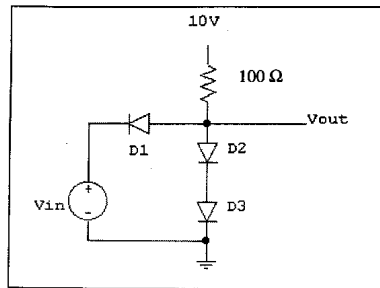
$$c) \quad PIV = V_m = 28.2V \quad 4$$

$$d) \quad V_r = \frac{V_m}{2fRC} = \frac{28.2}{2(50)(10k)(70\mu F)} = 0.4V \quad 6$$

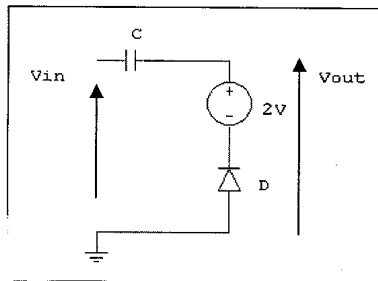
$$RC = 0.7s \gg \frac{1}{50}s = T \quad 3$$

$$\begin{aligned} e) \quad V_{DC} &\approx V_m - \frac{V_r}{2} = 28.2 - 0.2 \\ &= 28V \end{aligned} \quad 4$$

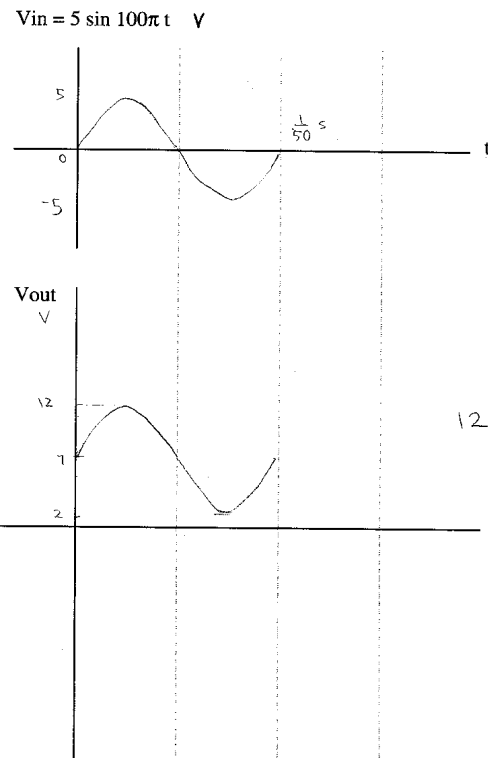
9. a) Plot the transfer curve  $V_{out}$  versus  $V_{in}$  for the following circuit ( $-2V \leq V_{in} \leq 2V$ ). Assume  $V_D = 0.7V$  when the diode is on. Show clearly the voltages. (12 marks)



- b) Sketch  $V_{in}$  and  $V_{out}$  for the following circuit. Assume the diode is ideal. Show clearly the voltage and time intercepts. (12 marks)

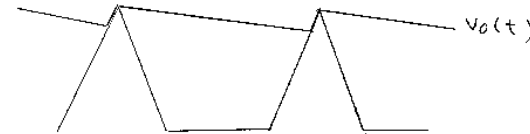
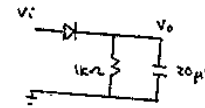


$$\begin{aligned}\omega &= 2\pi f \\ &= 100\pi \\ \therefore f &= 50 \text{ Hz} \\ T &= \frac{1}{50} \text{ s}\end{aligned}$$



9. In the ideal diode circuit,  $V_i$  is a 1 kHz triangular wave with 20V peak to peak (0V average).

- (a) Sketch  $V_o(t)$ . (6)  
(b) Show that the ripple voltage is roughly 0.5V. (8)  
(c) Show also that the peak inverse voltage (PIV) of the diode is 20V. (4)

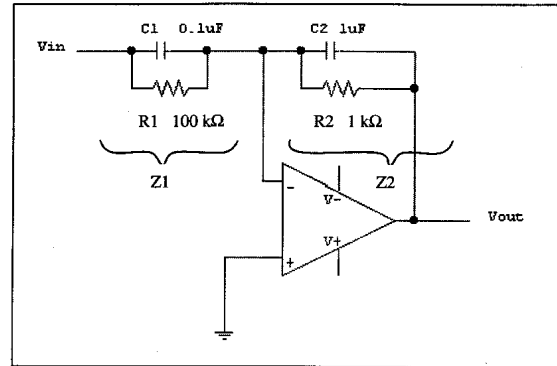


$$\begin{aligned}CR &= 20\mu \cdot 1k = 20ms \\ &\gg T = 1ms\end{aligned}$$

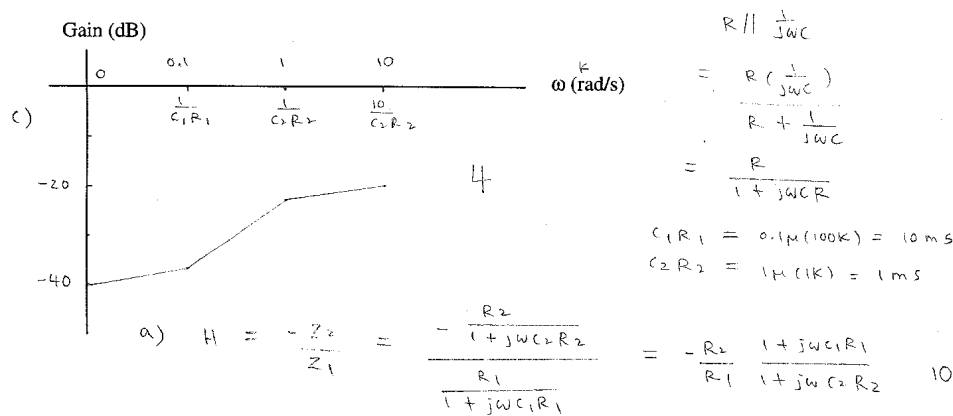
$$\begin{aligned}\therefore V_r &= \frac{V_m T}{CR} = \frac{10V (1m)}{20m} \\ &= 0.5V\end{aligned}$$

$$PIV = 2V_m = 20V$$

11. Given the following circuit diagram. Assume ideal Op Amp.



- a) Write the transfer function  $H(j\omega) = V_{out}(j\omega) / V_{in}(j\omega)$ . (10 marks)  
 Given :  $H = -Z_2 / Z_1$  for an inverting amp.  
 b) Show that  $|H(\omega)| = -40\text{dB}$  when  $\omega = 0$  and  $|H(\omega)| = -20\text{dB}$  when  $\omega = 10 / C_2 R_2$ . (12 marks)  
 Appropriate assumption will be accepted.  
 c) Sketch the gain  $|H(\omega)|$  versus the frequency. (4 marks)  
 Given :  $|H(\omega)| \approx -23\text{dB}$  when  $\omega = 1 / C_2 R_2$  and  $|H(\omega)| \approx -37\text{dB}$  when  $\omega = 1 / C_1 R_1$ .  
 d) What is the type of this filter? (2 marks)



b)  $\omega = 0$   $H = -\frac{R_2}{R_1} = -\frac{1k}{100k}$  or  $|H| = -40\text{dB}$

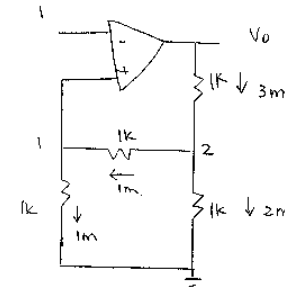
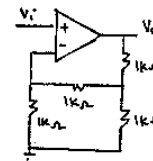
$\omega = \frac{10}{C_2 R_2}$   $H = -\frac{1}{100} \frac{1 + j \frac{10 C_1 R_1}{C_2 R_2}}{1 + j 10} = -\frac{1}{100} \frac{1 + j 100}{1 + j 10}$

$\approx -\frac{1}{10}$   $|H| = -20\text{dB}$

d) high pass filter

2

6. (a) In the ideal op amp circuit, if  $V_i = 1\text{V}$ , find  $V_o$ . (12)



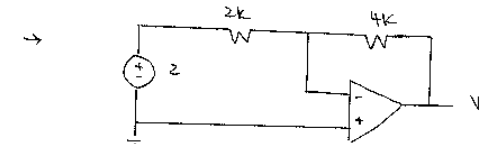
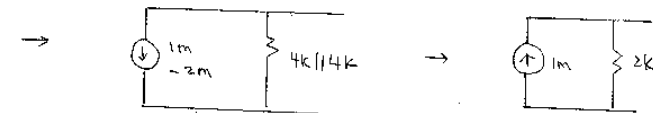
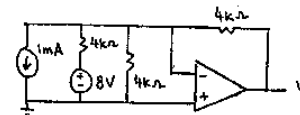
$V_o = 1k + 3m$

$+ 1k \times 2m$

$= 5V$

12

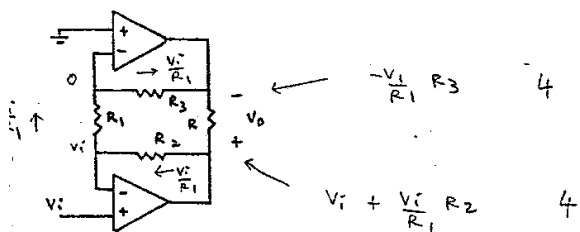
(b) In the ideal op amp circuit, show that  $V_o = -4\text{V}$ . (Hint: use source transform). (16)



$V_o = -\frac{4k}{2k} 2 = -4V$

4

8. For the following circuit, assume ideal op amp, show that  $V_o = V_i (1 + R_2/R_1 + R_3/R_1)$ . (20)



$$\therefore V_o = V_i \left( 1 + \frac{R_2}{R_1} \right) - \left( -V_i \frac{R_3}{R_1} \right)$$

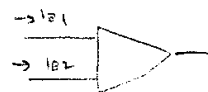
$$= V_i \left( 1 + \frac{R_2}{R_1} + \frac{R_3}{R_1} \right)$$

$$R_i \sim \infty$$

$$A < R_1$$

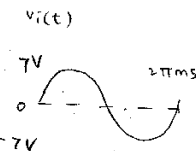
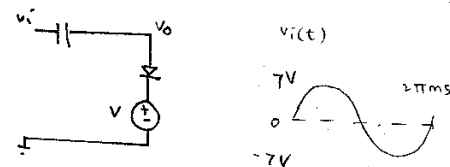
can be a difference  
amp

9. Explain briefly the following real op amp properties: (i) input offset voltage, (ii) input bias current, (iii) slew rate. (9)

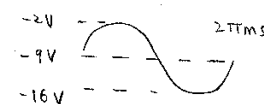


slew rate ~ maximum rate of change  
of  $V_o$

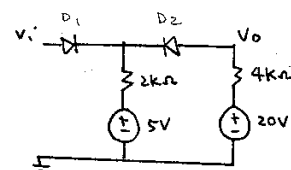
6. (a) If  $V_i(t) = 7 \sin 1000t$  V and  $V = -2$  V, sketch  $V_i(t)$  and  $V_o(t)$  for the following ideal diode circuit. Show clearly the voltages and time in your sketch. (12)



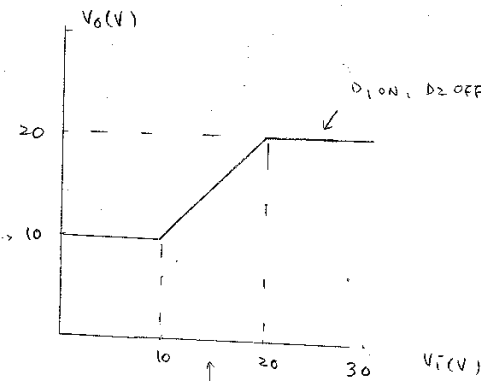
$V_o(t)$



(b) Plot  $V_o$  versus  $V_i$  for  $0V \leq V_i \leq 30V$  for the following ideal diode circuit. Show clearly all the voltages in your sketch. (13)

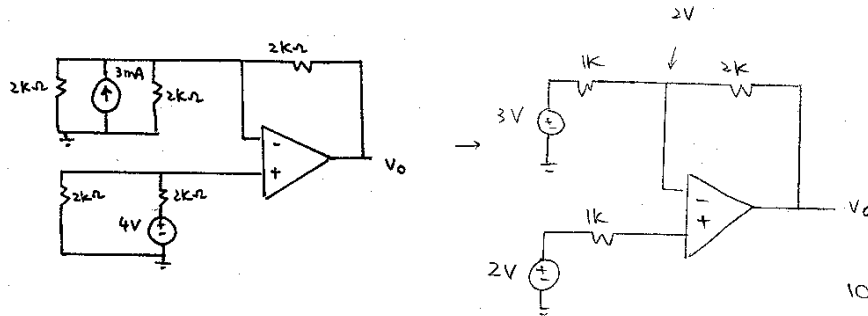


$$V_o = 5 + \frac{(20-5)2k}{2k+4k}$$



$D_1$  ON,  $D_2$  ON  
 $V_o = V_i$

8. (a) Find  $V_o$  for the following ideal op amp circuit. (14)



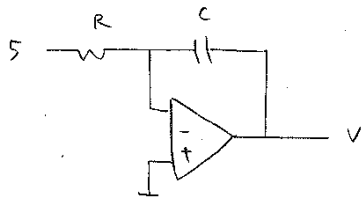
$$\therefore \frac{3-2}{1k} = \frac{2-V_o}{2k}$$

$$\therefore V_o = 0V$$

4

- (b) Design an ideal op amp circuit to obtain the solution of the following differential equation:

$$5 \frac{dv}{dt} + \frac{5}{7} = 0. \quad (14)$$



$$\frac{5}{R} = -C \frac{dv}{dt}$$

$$\therefore \frac{dv}{dt} + \frac{5}{CR} = 0$$

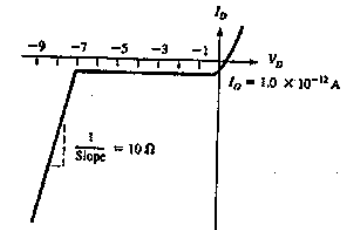
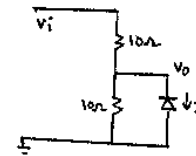
$$\text{Let } CR = 35 \quad \therefore \quad R = 35k\Omega \\ C = 1mF$$

14

10. In the following diode circuit, the diode has the reverse characteristics as shown.

- (a) Find  $V_o$  and  $I$  if  $V_i = 4V$ . (9)

- (b) Show that  $I = 0.2A$  if  $V_i = 20V$ . (17)



$$V_i = 4V$$

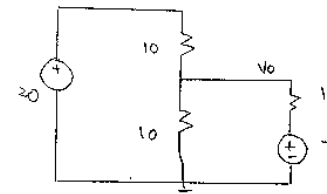
$$V_o = 2V$$

$$I = I_0 = 1pA$$

5

4

$$V_i = 20V$$



$$\therefore \frac{20-V_o}{10} = \frac{V_o-7}{10} + \frac{V_o}{10}$$

$$\therefore V_o = 9V$$

$$\therefore I = \frac{9-7}{10} = 0.2A$$

6

8

3