

Midterm Examination

Solution and Marking Scheme

1. d (4 points)
2. a (4 points)
3. e (4 points)
4. (14 points total)

- a) For a given program, let N denote the total number of instructions, N_A the number of class A instructions, N_B the number of class B instructions, and N_C the number of class C instructions.

CPU time = CPU clock cycles / clock rate

$$\begin{aligned}\text{CPU time on M1 using C1} &= (4 N_A + 6 N_B + 8 N_C) / 400 \text{ msec} \\ &= (4 \times 0.3 + 6 \times 0.5 + 8 \times 0.2) N / 400 \text{ msec} \\ &= 5.8 N / 400 \text{ msec}\end{aligned}\quad (1.5 \text{ points})$$

$$\begin{aligned}\text{CPU time on M2 using C1} &= (2 \times 0.3 + 4 \times 0.5 + 3 \times 0.2) N / 200 \text{ msec} \\ &= 3.2 N / 200 \text{ msec}\end{aligned}\quad (1.5 \text{ points})$$

Thus, using C1, M1 is $6.4 / 5.8$ or $32 / 29$ times as fast as M2. (1.5 points)

- b) CPU time on M1 using C2 = $(4 \times 0.3 + 6 \times 0.2 + 8 \times 0.5) N / 400 \text{ msec}$
= $6.4 N / 400 \text{ msec}$ (1.5 points)

$$\begin{aligned}\text{CPU time on M2 using C2} &= (2 \times 0.3 + 4 \times 0.2 + 3 \times 0.5) N / 200 \text{ msec} \\ &= 2.9 N / 200 \text{ msec}\end{aligned}\quad (1.5 \text{ points})$$

Thus, using C2, M2 is $6.4 / 5.8$ or $32 / 29$ times as fast as M1. (1.5 points)

- c) CPU time on M1 using C3 = $(4 \times 0.5 + 6 \times 0.3 + 8 \times 0.2) N / 400 \text{ msec}$
= $5.4 N / 400 \text{ msec}$ (1.5 points)

C3 is the best choice since the CPU time for the program on M1 using C3 is the shortest. (1 point)

- d) CPU time on M2 using C3 = $(2 \times 0.5 + 4 \times 0.3 + 3 \times 0.2) N / 200 \text{ msec}$
= $2.8 N / 200 \text{ msec}$ (1.5 points)

C3 is the best choice since the CPU time for the program on M2 using C3 is the shortest. (1 point)

5. (10 points total)

Let N denote the total number of instructions in the program.

CPU time = CPU clock cycles / clock rate

CPU time on M1 = $N / 400$ msec (4 points)

CPU time on M2 = $(5 \times 0.2 + 4 \times 0.1 + 4 \times 0.5 + 3 \times 0.15 + 3 \times 0.05) N / 200$ msec
= $N / 50$ msec (4 points)

Thus, M1 is $400 / 50$ or 8 times as fast as M2. (2 points)

6. (10 points total)

This pseudoinstruction

```
ble $s0, $s1, L
```

can be implemented as

```
slt $t0, $s1, $s0
beq $t0, $zero, L
```

7. (15 points total)

```

      add $t1, $zero, $zero    # $t1 = i = 0
      add $t2, $t0, $zero      # $t2 = address of a[0]
Loop: slti $t3, $t1, 10        # $t3 = 1 if i < 10
      beq $t3, $zero, Exit     # Exit loop if i >= 10
      addi $t4, $t1, 1         # $t4 = i + 1
      sw   $t4, 0($t2)         # a[i] = i + 1
      addi $t1, $t1, 1         # $t1 = i + 1
      addi $t2, $t2, 4         # $t2 = $t2 + 4
      j    Loop
Exit:
```

8. (15 points total)

a)

Inputs			Outputs	
a	b	CarryIn	CarryOut	Sum
0	0	0	0	0
0	0	1	0	1
0	1	0	0	1
0	1	1	1	0
1	0	0	0	1
1	0	1	1	0
1	1	0	1	0
1	1	1	1	1

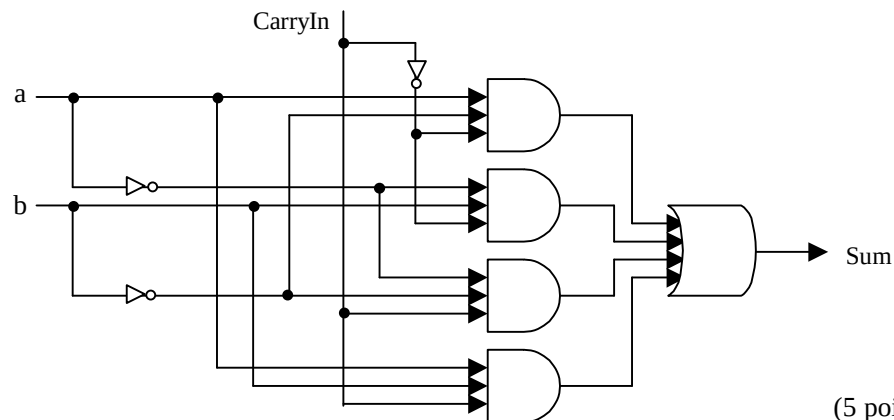
(5 points)

b) $\text{Sum} = (\underline{a} \cdot \underline{b} \cdot \underline{\text{CarryIn}}) + (\underline{a} \cdot b \cdot \underline{\text{CarryIn}}) + (a \cdot \underline{b} \cdot \text{CarryIn}) + (a \cdot b \cdot \text{CarryIn})$

(5 points)

[underline denotes NOT]

c)



(5 points)

9. (12 points total)

a) Bit 31 : 0 (1 point)

Bits 30-23 : 01111110 (2 points)

Bits 22-0 : 11111111111111111111 (2 points)

b) $x = -24$ (3 points)

c) With the biased notation, floating-point numbers can be compared in magnitude (e.g. for sorting) simply by performing integer comparison without having to compute the actual values of the floating-point numbers. (4 points)

10. (12 points total)

a) $2^{31} + 2^{27} + 2^{26} + 2^{25} + 2^{24} + 2^{23} + 2^{22} + 2^{21} + 2^{19} + 2^{18} + 2^{17} + 2^{16} + 2^{15} + 2^{14}$ (4 points)

b) $-2^{31} + 2^{27} + 2^{26} + 2^{25} + 2^{24} + 2^{23} + 2^{22} + 2^{21} + 2^{19} + 2^{18} + 2^{17} + 2^{16} + 2^{15} + 2^{14}$ (4 points)

c) Sign bit = 1

Exponent field = 00011111_{two} = 31_{ten}

Significand field = 1101111110000000000000

Decimal value = $-(1 + 2^{-1} + 2^{-2} + 2^{-4} + 2^{-5} + 2^{-6} + 2^{-7} + 2^{-8} + 2^{-9}) \times 2^{31-127}$ (4 points)